

**4 (a) (i)** Express as a single logarithm

$$\log_a 36 - \frac{1}{2} \log_a 81 + 2 \log_a 4 - 3 \log_a 2$$

**[3 marks]**

**4 (a) (ii)** Hence find the value of  $a$ , given

$$\log_a 36 - \frac{1}{2} \log_a 81 + 2 \log_a 4 - 3 \log_a 2 = \frac{3}{2}$$

**[1 mark]**

**4 (b)** Solve the equation  $9e^{2x} = 16$ , expressing your answer in the form  $\ln p$  where  $p$  is a rational number.

**[2 marks]**

**9** A curve has equation  $y = e^{2x}$

Find the coordinates of the point on the curve where the gradient of the curve is  $\frac{1}{2}$

Give your answer in an exact form.

**[5 marks]**

**10** David has been investigating the population of rabbits on an island during a three-year period.

Based on data that he has collected, David decides to model the population of rabbits,  $R$ , by the formula

$$R = 50e^{0.5t}$$

where  $t$  is the time in years after 1 January 2016.

**10 (a)** Using David's model:

**10 (a) (i)** state the population of rabbits on the island on 1 January 2016;

**[1 mark]**

**10 (a) (ii)** predict the population of rabbits on 1 January 2021.

**[1 mark]**

- 10 (b) Use David's model to find the value of  $t$  when  $R = 150$ , giving your answer to three significant figures.

[2 marks]

- 10 (c) Give **one** reason why David's model may **not** be appropriate.

[1 mark]

- 10 (d) On the same island, the population of crickets,  $C$ , can be modelled by the formula

$$C = 1000e^{0.1t}$$

where  $t$  is the time in years after 1 January 2016.

Using the two models, find the year during which the population of rabbits first exceeds the population of crickets.

[3 marks]

- 2 A zoologist is investigating the growth of a population of red squirrels in a forest.

She uses the equation  $N = \frac{200}{1 + 9e^{-\frac{t}{5}}}$  as a model to predict the number of squirrels,

$N$ , in the population  $t$  weeks after the start of the investigation.

What is the size of the squirrel population at the start of the investigation?

Circle your answer.

[1 mark]

5                      20                      40                      200

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